## Number Theory Seminar

Friday, September 6th, 2019

11:30 am in Hume 321

## Zhenchao Ge

## Essential Components in $\mathbb{F}_p[t]$

## ABSTRACT

A subset H of non-negative integers is called an essential component, if  $\underline{d}(A + H) > \underline{d}(A)$  for all  $A \subset \mathbb{N}$  with  $0 < \underline{d}(A) < 1$ , where  $\underline{d}(A)$  is the lower asymptotic density of A. How sparse can an essential component be? The best known result of this problem is due to Ruzsa. Here, we generalize the problem to the additive group  $(\mathbb{F}_p[t], +)$ . Our result is analogous to but more precise than Ruzsa's result in the integers. We also construct an explicit example of an essential component in  $\mathbb{F}_p[t]$  with a small counting function, based on an argument of Wirsing. This is joint work with Thái Hoàng Lê.