

# Research Talk

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## Dichromatic number and fractional chromatic number

### ABSTRACT

Given an undirected graph  $G$ , the chromatic number  $\chi(G)$  is the minimum order of partitions of  $V(G)$  into independent sets. Given a directed graph  $D$ , a vertex set is acyclic if it does not contain a directed cycle. The chromatic number  $\chi(D)$  is the minimum order of partitions of  $V(G)$  into acyclic sets. The dichromatic number of an undirected graph  $G$ , denoted by  $\overrightarrow{\chi}(G)$ , is the maximum chromatic number over all its orientations. Erdős and Neumann-Lara proved that  $C_1 \frac{n}{\log n} \leq \overrightarrow{\chi}(K_n) \leq C_2 \frac{n}{\log n}$  for some constants  $C_1, C_2$ . They conjectured that if the dichromatic number of a graph is bounded, so does its chromatic number.

Let  $\mathcal{I}(G)$  be the set of all independent sets of  $G$ , and let  $\mathcal{I}(G, x)$  be the set of all those independent sets which include vertex  $x$ . For each independent set  $I$ , define a nonnegative real variable  $x_I$ . The fractional chromatic number  $\chi_f(G)$  is the minimum value of  $\sum_{I \in \mathcal{I}(G)} x_I$ , subject to  $\sum_{I \in \mathcal{I}(G, x)} x_I \geq 1$  for each vertex  $x$ . We prove that there is a constant  $C$  such that for any graph  $G$ , we have  $\overrightarrow{\chi}(K_n) \geq C \frac{N}{\log n}$ .

This is joint work with Professor Bojan Mohar in Simon Fraser University.