ANALYSIS SEMINAR

UNIFORM APPROXIMATION UNDER CONSTRAINTS FOR CONTINUOUS VECTOR-VALUED FUNCTIONS

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Wednesday, February 16, 2005 in Room 331 at 3:00 pm

Abstract: The talk will discuss approximations with constraints on the range and on the support. For any $\varepsilon > 0$, the approximant u_{ε} of u (continuous maps defined on a topological space T) is required to take locally (on neighborhoods) values into finite dimensional subspaces, and to satisfy the restrictions

 $\sup_{t\in T} \|u(t) - u_{\varepsilon}(t)\| < \varepsilon, \quad u_{\varepsilon}(T) \subset \operatorname{co}(u(T)), \quad \operatorname{supp} u_{\varepsilon} \subset \operatorname{int}(\operatorname{supp} u).$

The result obtained has very distinct applications: a generalization of the Tietze-Dugundji extension theorem, a new proof of the fixed point theorem of Schauder-Tihonov, and a density result with respect to the inductive limit topology.