

# Combinatorics Seminar

Friday, Oct. 9, 2009

2:00 pm in Hume 331

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## On the shell of some graphs

### ABSTRACT

Let  $G$  be a graph such that each vertex of  $G$  is contained in a  $(k + 1)$ -clique for a positive integer  $k$ . We define the **shell of  $G$** , denoted by  $Sh(G)$  as follows: The vertex set of  $Sh(G)$  consists of all distinct  $(k + 1)$ -cliques of  $G$  and two vertices in  $Sh(G)$  are adjacent if and only if the corresponding  $(k + 1)$ -cliques have  $k$  vertices in common. If  $k = 1$ ,  $Sh(G)$  will be the line graph of  $G$ . If  $G$  is a  $k$ -tree with at least  $k + 1$  vertices, each vertex of  $G$  is contained in a  $(k + 1)$ -clique. In this talk, we will focus our attention on the shell of  $k$ -trees. Some properties and results on independence polynomials of the shells of  $k$ -trees will be presented and some related research problems will be proposed.